Molecular Spins ... a new Frontier?

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Warning: this is a presentation of a Conjecture

which contains many plausible aspects, but also some questionable ones.

An experimental verification is at present not available.

Magnetic particles which we know reasonably well today

(meaning that we know both the spin S and the magnetic moment μ)

Leptons		Nucleons	Nuclides
e _{1/2}	-28024.952	¹ p _½ 42.57748 uud	$^{1}\text{H}_{\frac{1}{2}}$ 42.57748
$\mu_{1\!/_{\!2}}$	-135.539	0 n _{$\frac{1}{2}$} -29.16469 ddu	$^{2}\text{H}_{1}$ 6.53590
$\tau_{1/2}$	too short-lived	Hyperons	$^{3}\text{H}_{\frac{1}{2}}$ 45.41367
$V_{1/2}$	haha, catch me!	$\Lambda, \Sigma, X, \Omega$ too short-lived	$^{3}\text{He}_{\frac{1}{2}}$ 32.43410
	Hadrons	Photons	⁶ Li ₁ 6.26587
$\eta_{1\!/_{\!2}}$	too short-lived	ϕ_1 0.000000 (in vacuo)	etc. ≈ 81 of them

Notes: lower-right index is the spin S, the value is the gyromagnetic ratio $\gamma = \mu / hS$ *in MHz/T*

Could we have some more ???

What about magnetic properties of molecules?

Persistent magnetic properties conferred by incorporated magnetic particles:

- * All practical magnetic *materials* are presently based on presence of unpaired electrons
- * Some devices are based on persistent superconducting loops (BCS electron pairs)
- * NMR exploits nuclear magnetism (detectable also without resonance)

But could molecules with no magnetic particles also have magnetic moments?

Property	Particles	Diamagnetic molecules
Electric dipole, induced Electric dipole, permanent	Yes, tiny? tiny (CP)	Yes (electric polarizability) Yes (symmetry permitting)
Magnetic dipole, induced Magnetic dipole, permanent	? undetectable Yes (if S>0)	Yes (magnetic susceptibility) ??? What !!!

?!? Permanent magnetic moments in diamagnetic molecules ?!?

?!! Man, you must be CRAZY!!?

There would have to exist persistent current loops inside the electron shell!

The Conjecture:

There may, and do, exist

persistent electron current loops
in molecular electronic shells, giving rise to

intrinsic molecular magnetism,
unrelated to any incorporated magnetic
particles, nor to any induced currents

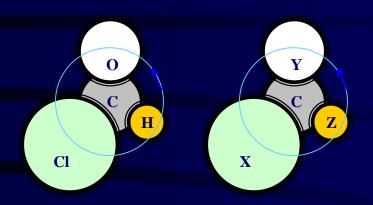
- Question: Why should such currents exist?
- Answer: Why not? Nothing forbids them!

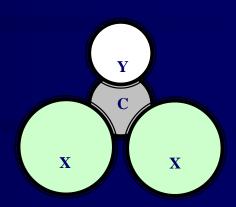
But let me try and tackle the query Why yes?

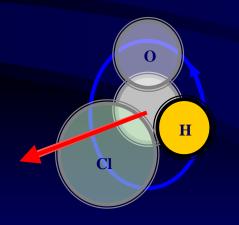
Molecular symmetry considerations

Circular asymmetry (axiality)

Circular symmetry (anaxiality)







Axiality & mirror reflections

Note:

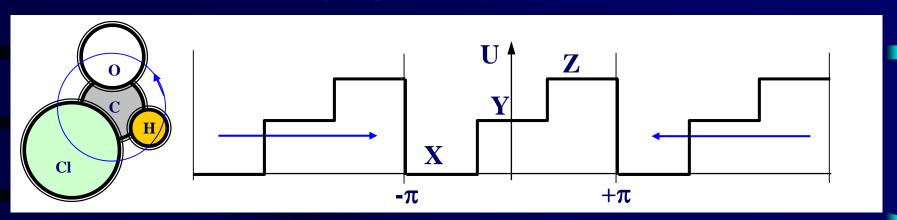
axiality is **not** chirality !!!

It does not make the molecule optically active.

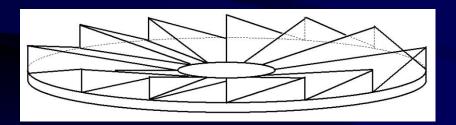
It does not lead to diastereomerism.

More symmetry considerations

Running loops one way and the other



There are an infinity of examples of circularly polarized mechanical devices

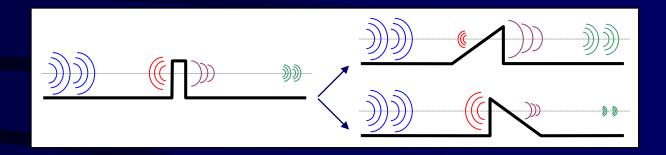


Fans, one-way clutches in all kinds of machinery, slipper clutches in motorbikes, etc, etc.

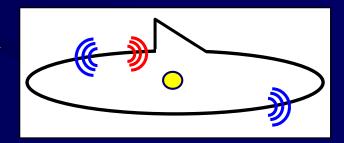
What about quantum analogies ?!?

Quantum Physics: traversing barriers (tunnelling)

- In these cases, the barrier asymmetry <u>does</u> matter (as it should)
- Note: wavefunctions are **pre-constructed** from the incident wave, the **reflected wave**, the **transmitted wave**, and perhaps a near transient; only coefficients are adjusted to match the Schrödinger equation.



- It is easy to close the linear path into an asymmetric circular loop:
- Shouldn't the asymmetry still matter !?



A fallacy in the standard handling of bound states

In molecules,

standing waves are **assumed** even **before** facing the eigenvalue problem. But in such multi-body systems, this may be too restrictive!

$$ih \frac{d}{dt} \Psi(s,t) = H\Psi(s,t) \longrightarrow \Psi(s,t) = exp\left(-i\frac{E}{h}t\right)\psi(s) \Longrightarrow H\psi(s) = E\psi(s)$$

For the ultra-simplified case of electron on a loop orbital, we might get:

$$ih \frac{d}{dt} \Psi(\phi, t) = -\frac{h^2}{2G} \frac{\partial^2}{\partial \phi^2} \Psi(\phi, t) + U(\phi) \Psi(\phi, t)$$

$$\Psi(\phi, t) = \exp\left(-i\frac{E}{h}t\right) \psi(\phi) \qquad \Rightarrow \qquad \frac{h^2}{2G} \frac{\partial^2 \psi(\phi)}{\partial \phi^2} + U(\phi) \psi(\phi) = E\psi(\phi)$$

$$\Psi_{\pm}(\phi, t) = \exp\left(-i\frac{E_{\pm}}{h}\left(t \pm \frac{\phi}{v}\right)\right) \psi_{\pm}(\phi) \qquad \Rightarrow \qquad H(\phi) \psi_{\pm}(\phi) = E_{\pm} \psi_{\pm}(\phi)$$

Notes: s ... all the space-like generalized coordinates, φ ... azimuth angle in a loop path

So, what if, for example, $E_{\perp} < E_{\perp}$? Then E_{\perp} is the ground state, occupied by an electron pair, and the molecule hosts a persistent current. This is necessarily the case when the molecule has no circular symmetry

Loop orbitals and "classical" orbitals

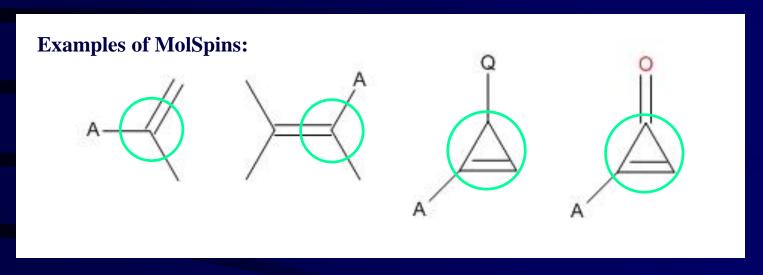
- Classical orbitals (atomic, Slater) are legitimate solutions in simplified situations void of circularity (1 or 2 atoms)
- Loop orbitals are legitimate solutions in simplified situations with circular arrangements (this requires a minimum of three different atoms)
- It is true that the manifold generated by all functions $\psi(s)$ is L_2 -complete in the space $\{s\}$, but it is NOT complete in $\{s,t\}$. The time-dependent Schrödinger equation has a broader set of solutions!
- Since atomic orbitals are combined in many ways to form various molecular shell approximations (LCAO, SCF-LCAO, ..., DFT), these combinations should include also loop orbitals. In practice, we are the ones who builds, artfully, the molecular Hilbert space.

Why we never saw so far such molecular magnetic moments (MMM)?

- Maybe simply because we were not looking for them
- Most of their bulk effects average out due to molecular tumbling
- They are *probably* small compared to induced effects such as the bulk magnetic susceptibility μ
- In solids, deviations of the μ tensor from its liquid-state value are likely to be ascribed to packing, small structural deviations, etc
- Last but not least: nobody used the best tool to look for persistent magnetic dipoles which, of course, is Magnetic Resonance

Consequences I

In the case of small molecules, we might have new magnetic particles (molecular spins) with which to do Molecular Magnetic Resonance (MMR)



Estimates of gyromagnetic ratios: very uncertain, my early guesses indicate << 0.1 MHz/Tesla

To search for the resonances, we will probably need: highest possible fields should be used (≥ 1 GHz), in combination with extremely broad-band probes

Differences in the relevant Physics

MMR physics versus that of NMR and EPR

The differences are bound to be considerable, since some fortuitous particle properties are absent:

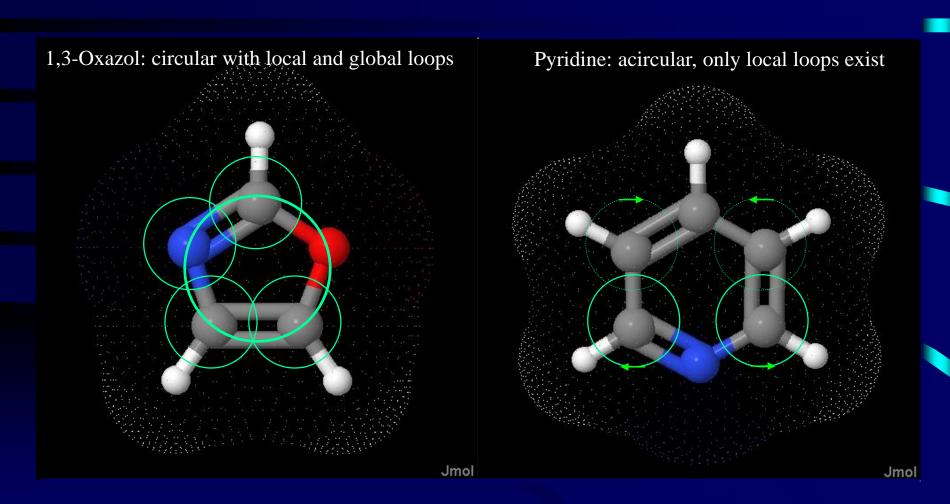
- * Magnetic moment and spin do not need to be aligned (!)
- * Magnetic moment might be spin-state dependent (!)
- * Interaction with molecular motions is bound to be very strong
- * Abstracted Spin Hamiltonian (Wes Anderson) is not applicable
- * Unlike in NMR/EPR, spin is likely to be just a perturbation factor, not a dominant one, in any MMM-related phenomenon.

Consequently, any resonances are likely to be extremely broad making MMR more a playground for chemical physicists.

But: one never knows!!!

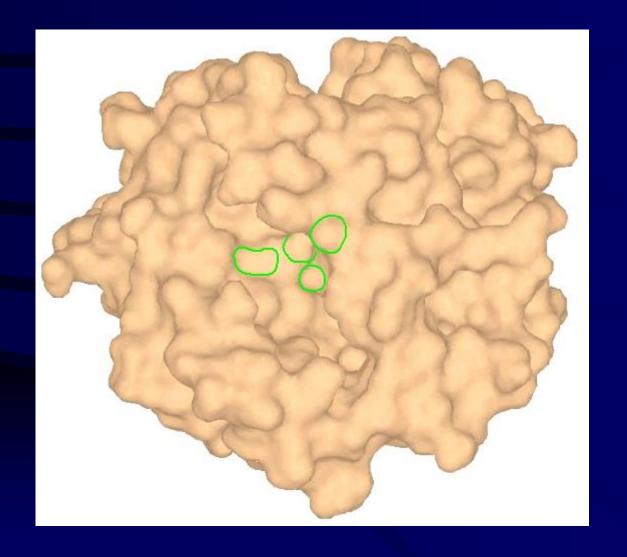
Global and Local circularity effects

Local current loops may exist even when, due to symmetry, the whole molecule can not have a magnetic dipole moment



Current loops distribution in large molecules

Only a few are drawn but they might constitute an intricate network



Consequences II

In Quantum Chemistry, loop currents might remove a roadblock:

DFT (Density-Function Theory)

 \Rightarrow

CCDFT (Charge & Current Density-Function Theory)

... Some more potential benefits for NMR:

improved predictions of NMR parameters

(shifts and coupling constants)

which are stuck at about ± 0.2 ppm since 20 years and improved only by a factor of 2 over more than 50 years, despite the enormous progress of computer technology.

